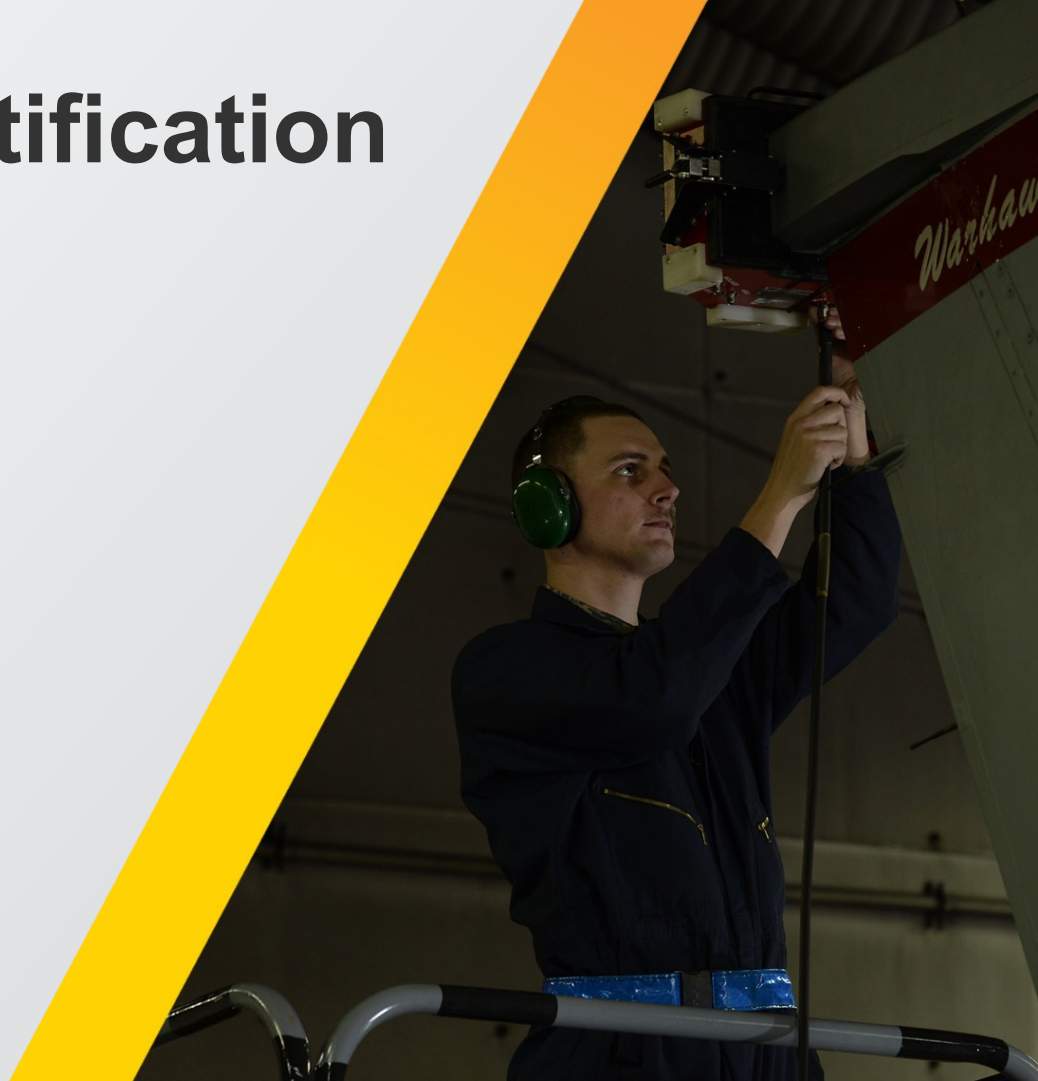


RWR Emitter Identification

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- **5 Aug 2021**





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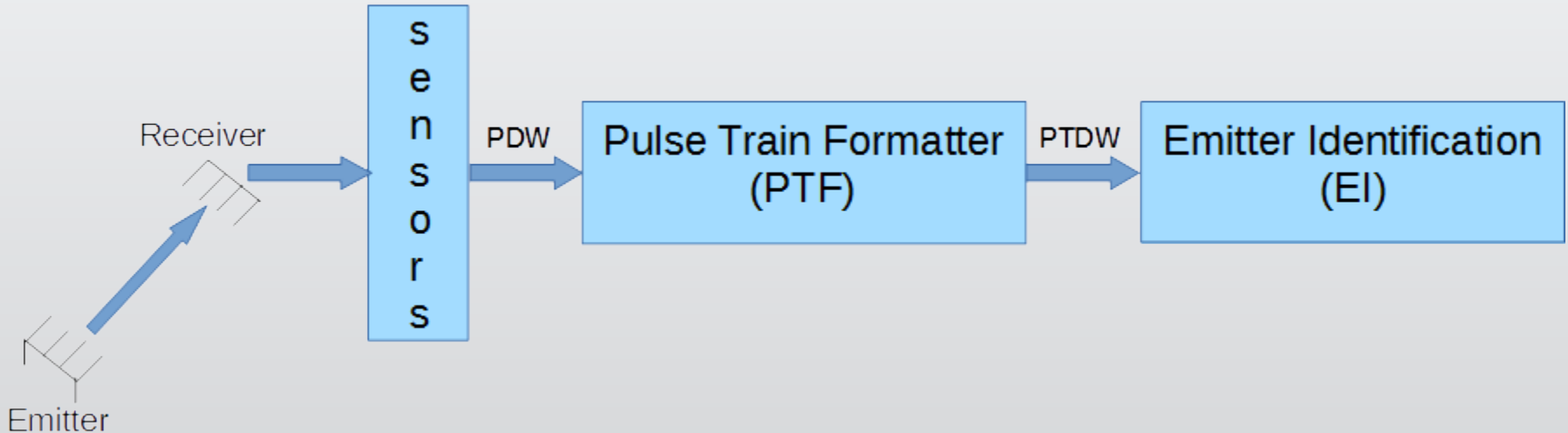
Presenter:

Arthur Schwarz
slipbits@slipbits.com



What is a Radar Warning Receiver

- A conceptual view of an RWR



We are interested in optimizing the EI

Goals

- Rapid identification of an emitter.
- Using all Emitters for any theater.
- Increase time/space scalability.
 - Linear growth.

Goals

Search Techniques

- Hashing
- Binary Search – focus of presentation
- Fuzzy Indexing

Goals

Hash Function Techniques

- Perfect HF, HF, Minimally Perfect HF
- HF
 - In theory yields a $O(1)$ performance.
 - Single item 100 probes
$$O(1) = 1.1 = \frac{100}{1000}$$
 - Actual performance depends on HF.
 - Size is $\approx 1.5 \#$ items, 1000 items, 1500 cells.

Assumptions

- Total of 4096 (2^{12}) virtual emitters
 - Each mode of a multi-mode emitter becomes a virtual emitter
 - 4096 virtual emitters can represent < 4096 real emitters
- The PTDW is the sole source of emitter data

Assumptions

- PTDW Parameters
 - Polarization (8 values == $\log_2 8 = 3$ bits)
 - Modulation type (16 values == $\log_2 16 = 4$ bits)
 - Frequency (f) = 2^{13} intervals = 13 bits
 - Pulse Width (τ_w) = 2^{10} intervals = 10 bits
 - Pulse Recurrence Interval (p) = 2^9 intervals = 9 bits

PTDW to Signature

- Pack all parameters into a Signature
 - Total size is 39 bits
 - Round-up to 48 bits – 3 16-bit words
- The set of Signatures are searchable
 - After sorting, a binary search is $\log_2 N$
 - For $N = 2^{17} = 131,072$ entries, this are 17 probes
 - 2^{20} bytes = 1,048,576 bytes
 - Hash search is $O(1)$

Signature Ambiguity

- Suppose two signatures are the same in the sorted list.
 - $S_i == S_{i+1}$
- This is an ambiguity and means that two virtual radars have the same PTDW parameters.
- A resolution policy is required.

Signature Overdetermined

- It is possible that one or more items in a signature can be removed without impeding the search.
 - The hardware for the item in question can be removed.
 - This translates into a reduction in cost.
- Building a radar is not the same as searching for one.

Summary

- Actual data must be used.
- Signatures yield fast EMI identification times.
- The time per probe is installation specific and can alter the effectiveness of the paradigm.

Analysis

- The picture is too pretty!
- There are two types of data
 - Discrete data whose values can be enumerated
 - Continuous data whose values can not be enumerated

Analysis

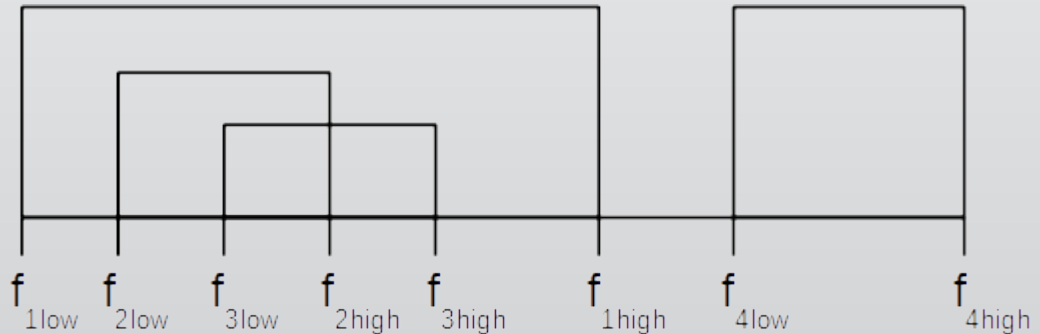
- Discrete data are things like:
 - Polarization (8 values): 3 bits = $\log_2 8$ bits
 - Modulation type (16 values): 4 bits = $\log_2 16$ bits
- Continuous data are things like:
 - Frequency (f)
 - Pulse Width (w)
 - Pulse Recurrence Interval (p)

Continuous Data (frequency)

- The frequencies need to be decimated.
 - Converted from continuous data an enumerable value
 - A 7 Mar 2019 AOC Webinar described a decimation algorithm
 - C++ code for this algorithm is at <https://slipbits.com/interval-search/>
 - Brute force takes $> O(n^3)$
 - Interval Analysis takes $O(3n + 2n \log_2 2n)$ steps

Range Decimation Overview

- Suppose we have four frequency ranges
 - f_1, f_2, f_3, f_4
- And
 - f_2 and f_3 are wholly contained in f_1 ,
 - f_2 intersects f_3 , and
 - f_4 is disjoint
- Graphically

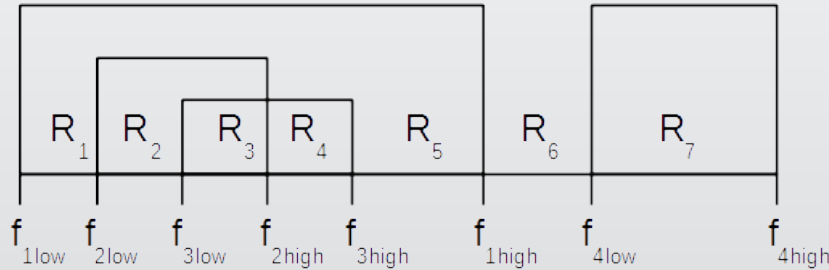


Range Decimation Overview

- Frequency intervals can not be used.
 - No sort order for a binary search.
 - A linear search is required.
- Ranges – unique intervals
 - Between $[f_i \text{start}, f_{(i+1)} \text{start})$, $[f_i \text{end}, f_{(i+1)} \text{start})$, etc.
- Ranges define non-overlapping frequencies.
 - Ranges are ordered ($R_i < R_{i+1}$).
 - A binary search can be done on enumerable ranges.

Range Decimation Overview

- This example decomposes.



- The regions are disjoint
 - An emitter can be in one or more frequency ranges
 - Range boundaries are coincident to frequency boundaries.

Range Decimation Overview

Range Sorting

- With a precedence order ranges can be sorted.
- Since all ranges, R , are disjoint:
 - Finding an f in any R is unique. f can not be in more than one range.

Time and Space

- Actual numbers for all values are based on the statistics of the EMI objects used.
 - My values are just poor guesses.
- The total number of signatures, 2^{17} , assumes that each of 4096 emitters have 32 signatures.
 - Signature search is 17 probes.
 - Maximum is $17 + 13 + 10 + 9 = 49$ probes

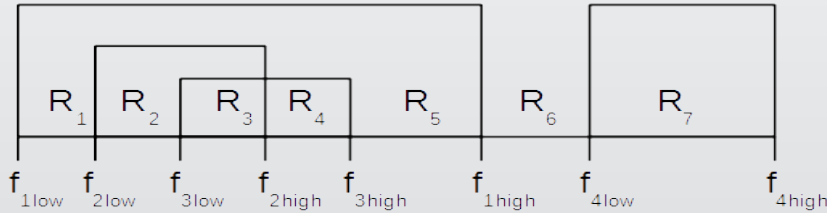
Order 1 probes

- The Range sizes have been variable.
 - Ranges are a subset of a frequency interval.
- Suppose we used fixed size Ranges.
 - Then a probe is: $\text{int}(f/\text{width}) = 1$

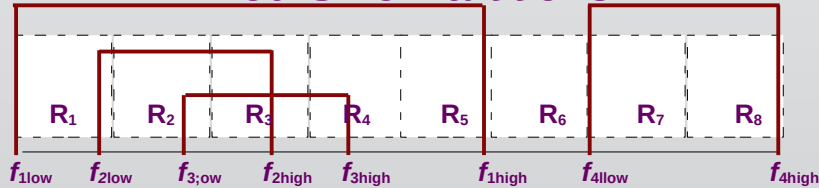
Order 1 probes

- Signatures may have ambiguities

Ideal Partitions



Fixed Size Partitions



Order 1 probes

- The dashed lines represent fixed sized intervals.
- Some frequency intervals are not fully contained in a fixed sized interval.
- This misrepresents the emitters in the signature set and leads to false ambiguities.
- These ambiguities can not be resolved programmatically.
 - They require a search within an interval.

Order 1 probes

- With Ideal Partitions there area max of 49 probes.
 - Search interval tables $(f, w, p) = (13, 10, 9)$
 - Search Signature list (17)
- With Fixed Partitions there are:
 - Search interval tables $(f, w, p) = (1, 1, 1)$
 - Search Signature list (17) + bucket search
- If the bucket search < 29 :
 - Using Fixed Partitions is better than Ideal Partitions

Data Growth

- Worst case a new radar is not wholly contained in existing (f, w, p) intervals.
 - This increases the number of ranges by $6 = (2, 2, 2)$
 - The number of signatures increases by one for each range the new radar is in plus 1 for each existing radar in the new interval.